

$$1. f(x) = x^2 + 4$$

$$29 = x^2 + 4$$

$$25 = x^2$$

$$5 = x$$

$$f(5) = 29 \quad (5, 29) \text{ on } f(x)$$

$$f'(x) = 2x$$

$$f'(5) = 10$$

$$(f^{-1})'(29) = \frac{1}{10}$$

$$(29, 5) \text{ on } f^{-1}(x)$$

$$2. f(x) = 2x^3 + 5x + 1$$

$$8 = 2x^3 + 5x + 1$$

$$0 = 2x^3 + 5x - 7$$

$$x = 1$$

$$f'(x) = 6x + 5$$

$$f'(1) = 11$$

$$(f^{-1})'(8) = \frac{1}{11}$$

$$3. \sqrt{64.9}$$

$$f(x) = \sqrt{x}$$

$$x = 64$$

$$\Delta x = .9$$

$$\frac{dy}{dx} = \frac{1}{2} x^{-1/2}$$

$$dy = \frac{1}{2\sqrt{x}} dx$$

$$dy = \frac{1}{2\sqrt{64}} .9$$

$$dy = \frac{.9}{16}$$

$$\sqrt{64.9} = \sqrt{64} + \frac{.9}{8} = 8.056$$

$$4. f(x) = 2x^3 - 3$$

$$f'(x) = 6x^2$$

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

$$x_2 = 1 - \frac{f(1)}{f'(1)}$$

$$= 1 - \frac{(-1)}{6} = \frac{7}{6}$$

$$x_3 = x_2 - \frac{f(x_2)}{f'(x_2)}$$

$$x_3 = \frac{7}{6} - \frac{\frac{505}{216} - 3}{4 \cdot \frac{7}{6}} = \frac{505}{441} \approx 1.145$$

$$x_4 = 1.145$$