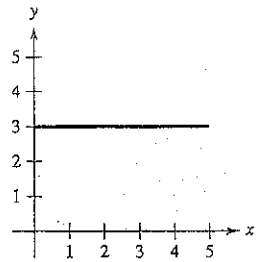
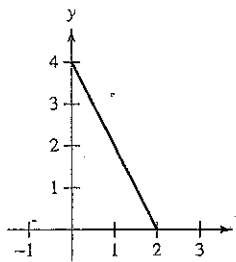


In Exercises 13–22, set up a definite integral that yields the area of the region. (Do not evaluate the integral.)

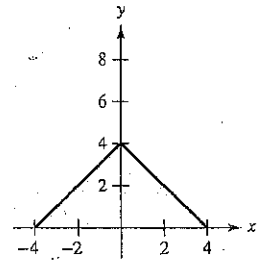
13.  $f(x) = 3$



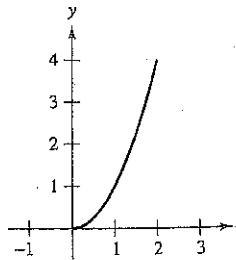
14.  $f(x) = 4 - 2x$



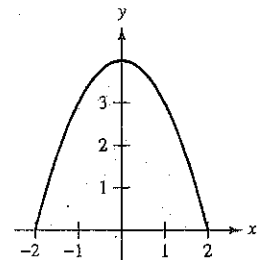
15.  $f(x) = 4 - |x|$



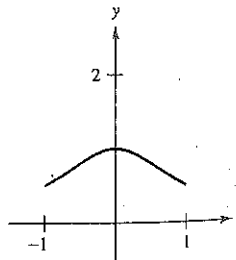
16.  $f(x) = x^2$



17.  $f(x) = 4 - x^2$



18.  $f(x) = \frac{1}{x^2 + 1}$



SECTION 4.3 Riemann Sums and Definite Integrals 273

41. Given  $\int_0^5 f(x) dx = 10$  and  $\int_5^7 f(x) dx = 3$ , find

(a)  $\int_0^7 f(x) dx$ .

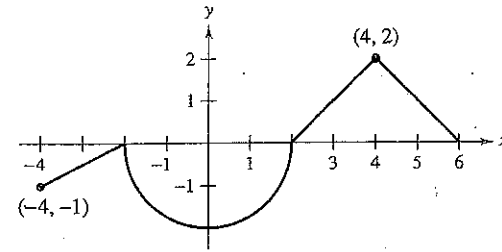
(b)  $\int_5^0 f(x) dx$ .

(c)  $\int_5^5 f(x) dx$ .

(d)  $\int_0^5 3f(x) dx$ .

45. **Think About It** The graph of  $f$  consists of line segments and a semicircle, as shown in the figure. Evaluate each definite integral by using geometric formulas.

- (a)  $\int_0^2 f(x) dx$
- (b)  $\int_2^6 f(x) dx$
- (c)  $\int_{-4}^2 f(x) dx$
- (d)  $\int_{-4}^6 f(x) dx$
- (e)  $\int_{-4}^6 |f(x)| dx$
- (f)  $\int_{-4}^6 [f(x) + 2] dx$



In Exercises 5–26, evaluate the definite integral of the algebraic function. Use a graphing utility to verify your result.

- 5.  $\int_0^1 2x dx$
- 6.  $\int_2^7 3 dv$
- 7.  $\int_{-1}^0 (x - 2) dx$
- 8.  $\int_2^5 (-3v + 4) dv$
- 9.  $\int_{-1}^1 (t^2 - 2) dt$
- 10.  $\int_1^3 (3x^2 + 5x - 4) dx$
- 11.  $\int_0^1 (2t - 1)^2 dt$
- 12.  $\int_{-1}^1 (t^3 - 9t) dt$
- 13.  $\int_1^2 \left(\frac{3}{x^2} - 1\right) dx$
- 14.  $\int_{-2}^{-1} \left(u - \frac{1}{u^2}\right) du$
- 15.  $\int_1^4 \frac{u - 2}{\sqrt{u}} du$
- 16.  $\int_{-3}^3 v^{1/3} dv$
- 17.  $\int_{-1}^1 (\sqrt[3]{t} - 2) dt$
- 18.  $\int_1^8 \sqrt{\frac{2}{x}} dx$
- 19.  $\int_0^1 \frac{x - \sqrt{x}}{3} dx$
- 20.  $\int_0^2 (2 - t)\sqrt{t} dt$
- 21.  $\int_{-1}^0 (t^{1/3} - t^{2/3}) dt$
- 22.  $\int_{-8}^{-1} \frac{x - x^2}{2\sqrt[3]{x}} dx$
- 23.  $\int_0^3 |2x - 3| dx$
- 24.  $\int_1^4 (3 - |x - 3|) dx$
- 25.  $\int_0^3 |x^2 - 4| dx$
- 26.  $\int_0^4 |x^2 - 4x + 3| dx$

In Exercises 27–32, evaluate the definite integral of the trigonometric function. Use a graphing utility to verify your result.

- 27.  $\int_0^{\pi} (1 + \sin x) dx$
- 28.  $\int_0^{\pi/4} \frac{1 - \sin^2 \theta}{\cos^2 \theta} d\theta$
- 29.  $\int_{-\pi/6}^{\pi/6} \sec^2 x dx$
- 30.  $\int_{\pi/4}^{\pi/2} (2 - \csc^2 x) dx$
- 31.  $\int_{-\pi/3}^{\pi/3} 4 \sec \theta \tan \theta d\theta$
- 32.  $\int_{-\pi/2}^{\pi/2} (2t + \cos t) dt$