

1. What is the area of the region between the graphs of $y = x^2$ and $y = -x$ from $x = 0$ to $x = 2$?

- (A) $\frac{2}{3}$ (B) $\frac{8}{3}$ (C) 4 (D) $\frac{14}{3}$ (E) $\frac{16}{3}$

2. The area of the region enclosed by the graph of $y = x^2 + 1$ and the line $y = 5$ is

- (A) $\frac{14}{3}$ (B) $\frac{16}{3}$ (C) $\frac{28}{3}$ (D) $\frac{32}{3}$ (E) 8π

3. The area of the region enclosed by the graphs of $y = x$ and $y = x^2 - 3x + 3$ is

- (A) $\frac{2}{3}$ (B) 1 (C) $\frac{4}{3}$ (D) 2 (E) $\frac{14}{3}$

4. The area of the region in the first quadrant enclosed by the graph of $y = x(1-x)$ and the x -axis is

- (A) $\frac{1}{6}$ (B) $\frac{1}{3}$ (C) $\frac{2}{3}$ (D) $\frac{5}{6}$ (E) 1

5. If the region enclosed by the y -axis, the line $y = 2$, and the curve $y = \sqrt{x}$ is revolved about the y -axis, the volume of the solid generated is

- (A) $\frac{32\pi}{5}$ (B) $\frac{16\pi}{3}$ (C) $\frac{16\pi}{5}$ (D) $\frac{8\pi}{3}$ (E) π

6. A region in the first quadrant is enclosed by the graphs of $y = e^{2x}$, $x = 1$, and the coordinate axes. If the region is rotated about the y -axis, the volume of the solid that is generated is represented by which of the following integrals?

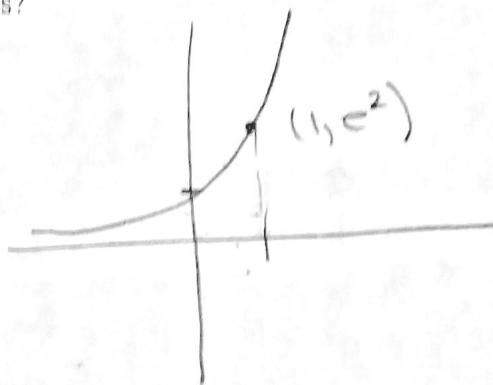
(A) $2\pi \int_0^1 x e^{2x} dx$

(B) $2\pi \int_0^1 e^{2x} dx$

(C) $\pi \int_0^1 e^{4x} dx$

(D) $\pi \int_0^e y \ln y dy$

(E) $\frac{\pi}{4} \int_0^e \ln^2 y dy$



$$2\pi \int_0^1 x e^{2x} dx$$

$$y' = 2x^{1/2} \quad 9x \int_{1/3}^7 \sqrt{1+9x} dx$$

7. Use your calculator to find the arclength of $y = 2x^{3/2}$ on $[\frac{1}{3} \leq x \leq 7]$.

$$\int = 112/3$$

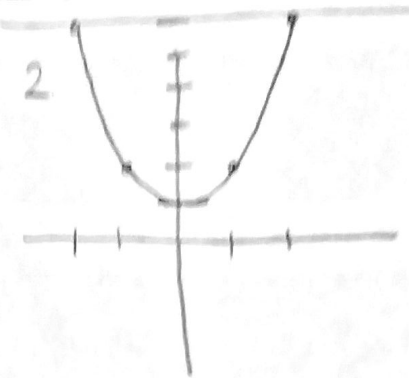
$$1. A = \int_0^2 x^2 - (-x) dx$$

$$A = \int_0^2 x^2 + x dx$$

$$\left[\frac{x^3}{3} + \frac{x^2}{2} \right]_0^2$$

$$\frac{8}{3} + 2$$

$$\frac{14}{3}$$



$$\int_{-2}^2 5 - (y^2 + 1) dy$$

$$\int_{-2}^2 4 - y^2 dy$$

$$\int_{-2}^2 4 - x^2 dx$$

$$\left[4x - \frac{x^3}{3} \right]_{-2}^2$$

$$8 - \frac{8}{3} - \left(-8 + \frac{8}{3} \right)$$

$$16 - \frac{16}{3}$$

$$\frac{48}{3} - \frac{16}{3} = \frac{32}{3}$$

3 (1,1) (2,3)

$$A = \int_1^3 x - (x^2 - 3x + 3) dx$$

$$A = \int_1^3 x - x^2 + 3x - 3$$

$$= \int_1^3 -x^2 + 4x - 3$$

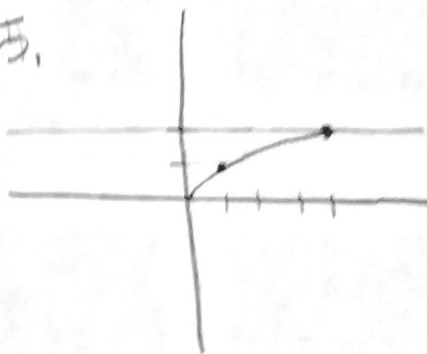
$$\left[-\frac{x^3}{3} + \frac{4x^2}{2} - 3x \right]_1^3$$

$$-\frac{27}{3} + \frac{36}{2} - 9 - \left[-\frac{1}{3} + \frac{4}{2} - 3 \right]$$

$$-9 + 18 - 9 + \frac{1}{3} - 2 + 3$$

$$\frac{1}{3}$$

5.



$$y = \sqrt{x}$$

$$y^2 = x$$

$$V = \pi \int_0^2 (y^2)^2 dy$$

$$V = \pi \int_0^2 y^4 dy$$

$$\pi \left[\frac{y^5}{5} \right]_0^2$$

$$\frac{32\pi}{5}$$